

## Data Summaries

Prof. Wells

STA 209, 2/3/23

# Outline

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- Consider a few extensions of `ggplot2`
- Discuss measurements of center and spread for quantitative data
- Use contingency tables to investigate relationships among categorical variables

## Section 1

# Summarizing Quantitative Data

## Exam Statistics

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What summarizing information would it be helpful to know in order to assess how well the class did?

- 1 What was the typical score (maybe average or median)?
- 2 How much variation was there in scores?
- 3 What was the shape of the data?
- 4 Were there any outliers?

## The Mean

The **mean** or average of a data set is one measure of *center*, obtained by adding all observed values and dividing by their number:

$$\bar{x} = \frac{x_1 + x_2 + \cdots + x_n}{n} = \frac{1}{n} \sum_{i=1}^n x_i$$

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```
mean(biketown_short$Distance_Miles)
```

```
## [1] 1.677599
```

## The Mean

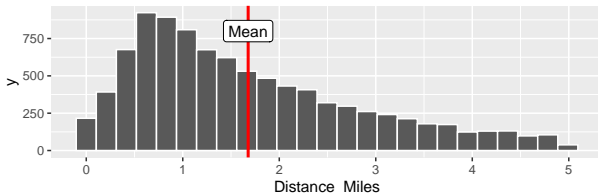
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## [1] 1.677599
```



- If the histogram were made of solid material, the mean would be the point along the horizontal axis where the solid is perfectly balanced.

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## [1] 1.39
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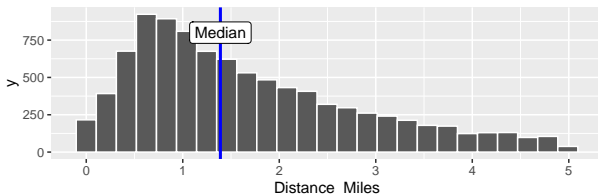
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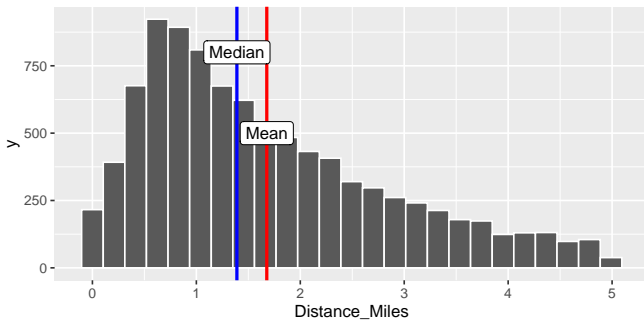
- The median corresponds to the line that divides a histogram into two equal area pieces.

## Mean, Median, and Skew

Both mean and median represent *typical* values for a data set.

## Mean, Median, and Skew

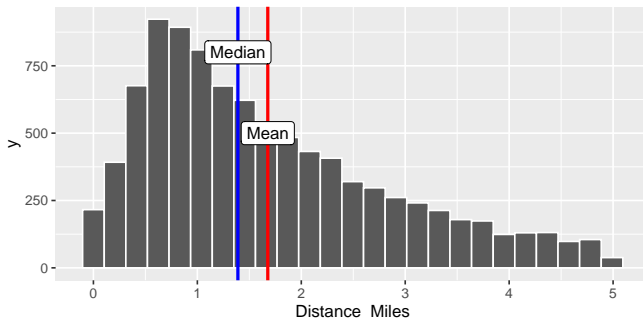
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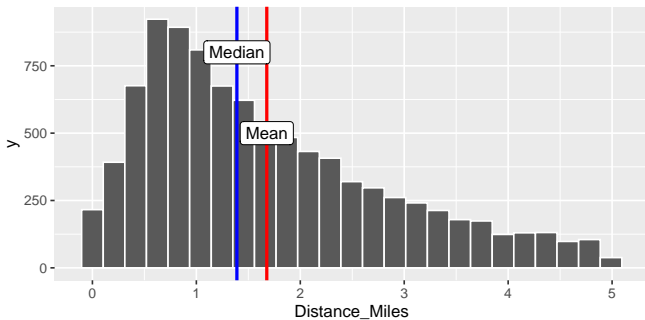
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  - Why?

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Consider two data sets, one with a large outlier and one without:

my_data_with_outlier	1	2	5	7	8	100
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The mean value of a dataset is very sensitive to outliers.

```
mean(my_data)
```

```
## [1] 5.5
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```
mean(my_data_with_outlier)
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## [1] 20.5
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The median, however, is not.

```
median(my_data)
```

```
## [1] 6
```

```
median(my_data_with_outlier)
```

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## [1] 6
```

## Measures of Variability

We'd like to assess how variable the data set is.

- Are values usually close to the mean, or are they spread out?

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Guess 1: Compute the average difference

$$\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})$$

Distance_Miles	Mean	Deviations
1.57	1.2	0.37
2.09	1.2	0.89
0.38	1.2	-0.82
0.86	1.2	-0.34
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Avg_Deviations
0

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Guess 2: Compute the average *squared* difference

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- This is called the **Population Variance**

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- This is called the **Population Variance**

Pop_Variance
0.3454

## Standard Deviation

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$$\text{Standard Deviation} = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$

## Visualizing Standard Deviation

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sd(biketown_short$Distance_Miles)
```

```
## [1] 1.172257
```



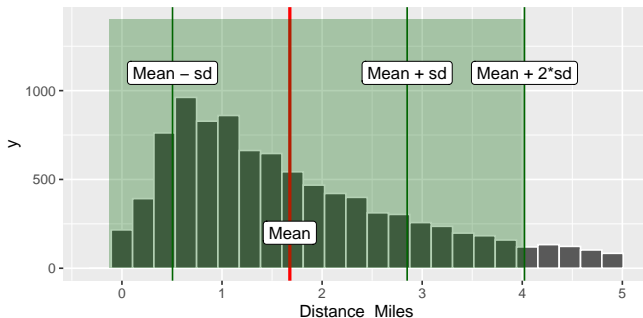
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```
quantile(biketown_short$Distance_Miles, c(.25, .75))
```

```
## 25% 75%
```

```
## 0.75 2.38
```

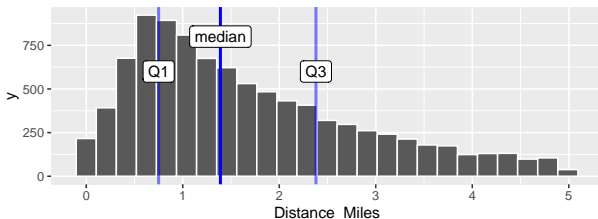
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```

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```



- The *IQR* is the distance between the 1st and 3rd quartile:  $IQR = Q3 - Q1$

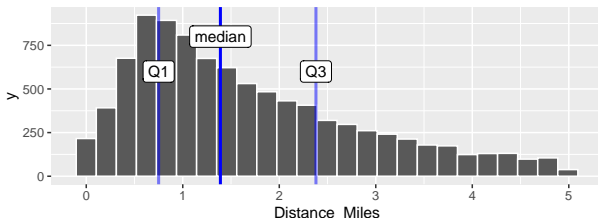
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```

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```



- The *IQR* is the distance between the 1st and 3rd quartile:  $IQR = Q3 - Q1$
- Comparing Median –  $Q1$  and  $Q3 - \text{Median}$  can show shape of distribution.

## Section 2

### Summarizing Categorical Data

# The Distribution of a Categorical Variable

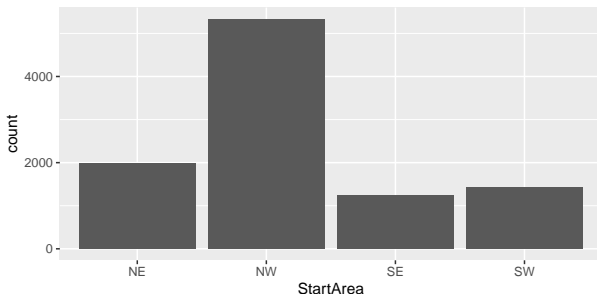
Distributions of categorical variables can be presented in tables and summarized in bar charts:



# The Distribution of a Categorical Variable

Distributions of categorical variables can be presented in tables and summarized in bar charts:

StartArea	NE	NW	SE	SW
n	1989	5334	1240	1424



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	Casual	Subscriber
NE	1141	848
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- Contingency tables can be created by applying the `table()` function to 2 columns of a data frame:

```
table(biketown$StartArea, biketown$PaymentPlan)
```

## Marginal Counts

- Suppose we want to recover the individual distribution of each variable in a table.

```
my_table <- table(biketown$StartArea, biketown$PaymentPlan)
```

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- Apply the `margin.table()` function to a table. Use 1 for the row variable and 2 for the column variable

```
margin.table(my_table, 1)
```

```
##  
##   NE   NW   SE   SW  
## 1989 5334 1240 1424
```

```
margin.table(my_table, 2)
```

```
##  
##      Casual Subscriber  
##      5354      4633
```

## Frequency Tables

Instead of comparing counts for each pair of values, we can consider the proportion of observations in each pair:



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my_table
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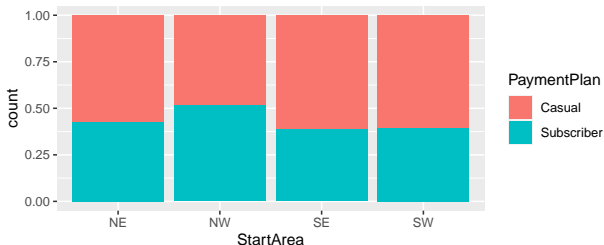
```
prop.table(my_table)
```

	Casual	Subscriber
NE	0.1142485	0.0849104
NW	0.2589366	0.2751577
SE	0.0762992	0.0478622
SW	0.0866126	0.0559728

## Row and Column Proportions

How do we create a table version of the segmented bar chart?

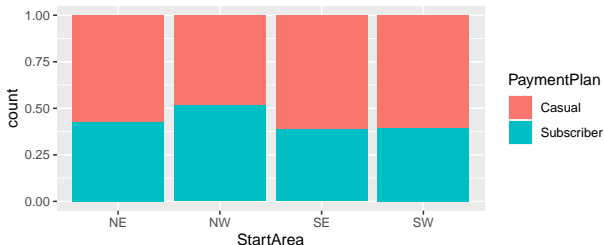
```
ggplot(biketown, aes(x = StartArea, fill = PaymentPlan)) + geom_bar(position = "fill")
```



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```
##
##      Casual Subscriber
## NE 0.5736551 0.4263449
## NW 0.4848144 0.5151856
## SE 0.6145161 0.3854839
## SW 0.6074438 0.3925562
```

- Each row gives breakdown of PaymentPlan by levels of StartArea

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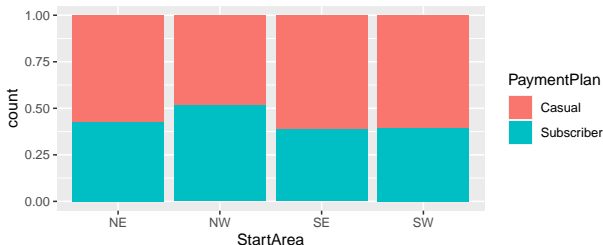
```
##
##           Casual Subscriber
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- Do column proportions?

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## SE 0.6145161  0.3854839  
## SW 0.6074438  0.3925562
```

```
prop.table(my_table, 2)
```

```
##  
##           Casual Subscriber  
## NE 0.2131117  0.1830348  
## NW 0.4830034  0.5931362  
## SE 0.1423235  0.1031729  
## SW 0.1615614  0.1206562
```

## Row and Column Proportions

Compare the results in the following tables:

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prop.table(my_table, 1)
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```

```
prop.table(my_table, 2)
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```
##
##           Casual Subscriber
##  NE 0.2131117  0.1830348
##  NW 0.4830034  0.5931362
##  SE 0.1423235  0.1031729
##  SW 0.1615614  0.1206562
```

And compare to the total proportion table:

```
prop.table(my_table)
```

```
##
##           Casual Subscriber
##  NE 0.11424852 0.08491038
##  NW 0.25893662 0.27515771
##  SE 0.07629919 0.04786222
##  SW 0.08661260 0.05597276
```



## Section 3

### Extending ggplot2

## Adding additional variables?

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But what can we do to simultaneously explore 3 variables?

- 1 3D Scatterplots; possible, but challenging to code and interpret (still limited to 2d display)
- 2 Map variables to additional aesthetics (beyond just  $x$  and  $y$ )
- 3 Show several 2D plots side-by-side.

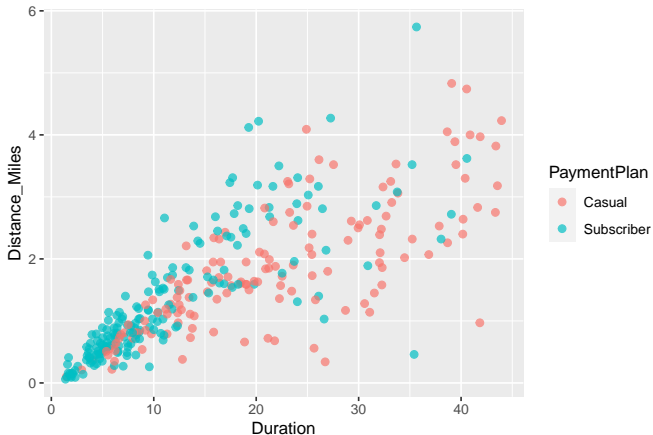
## Multiple Variables on 2d Plots

Does ride speeds depend on payment plan?

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```
ggplot(data = biketown_sample,  
       mapping = aes(x=Duration, y=Distance_Miles, color=PaymentPlan))+  
  geom_point(alpha = .7, size = 2)
```



# Facets

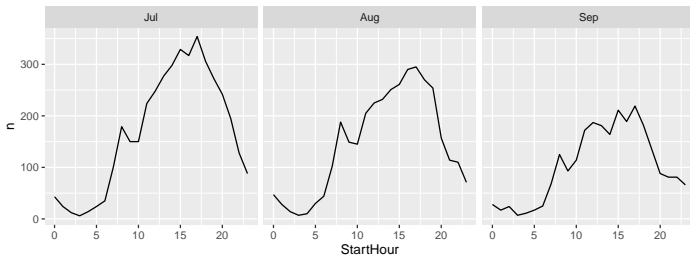
- Faceting is used to split one graphic into many smaller ones, based on the values of a categorical variable.



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- Faceting is used to split one graphic into many smaller ones, based on the values of a categorical variable.

```
ggplot(data = biketown2, mapping = aes(x = StartHour, y = n)) +  
  geom_line() +  
  facet_wrap(~Month, ncol = 3)
```

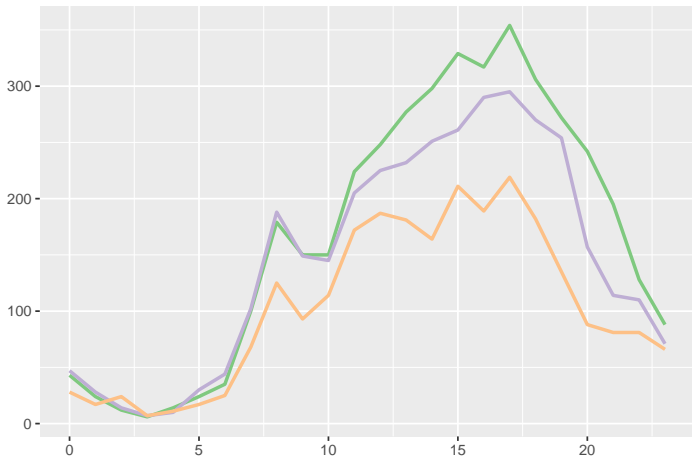


## Adding Context

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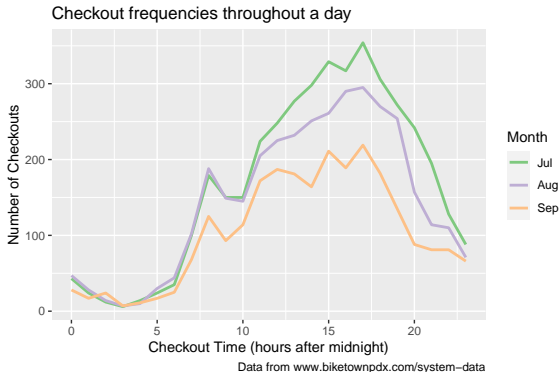
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```
ggplot(data = biketown2, mapping = aes(x = StartHour, y = n, color = Month)) +  
  geom_line( ) +  
  labs(x = "Checkout Time (hours after midnight)", y = "Number of Checkouts",  
        title = "Checkout frequencies throughout a day",  
        caption = "Data from www.biketownpdx.com/system-data")
```



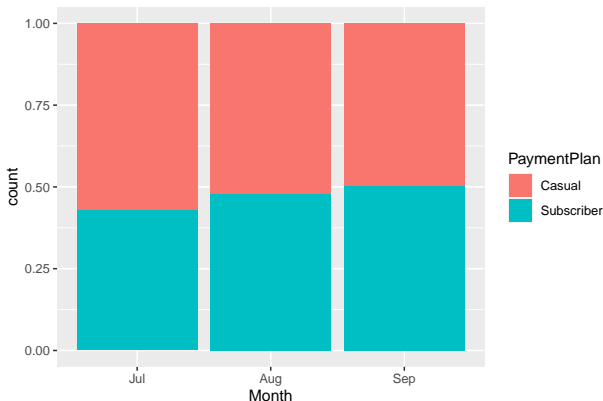
## Change Graphic Colors

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```
ggplot(data = biketown, mapping = aes(x = Month, fill = PaymentPlan)) +  
  geom_bar(position = "fill")
```



## Change Graphic Colors

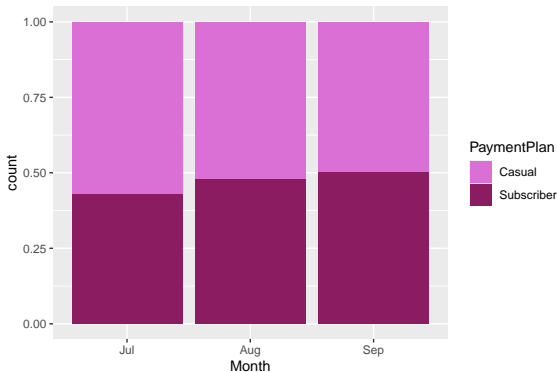
But it's possible to alter this by manually specifying colors.



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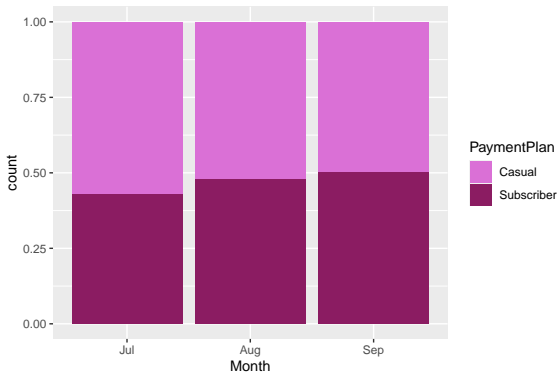
```
ggplot(data = biketown, mapping = aes(x = Month, fill = PaymentPlan)) +  
  geom_bar(position = "fill") +  
  scale_fill_manual(values = c("orchid", "maroon4"))
```



## Change Graphic Colors

But it's possible to alter this by manually specifying colors.

```
ggplot(data = biketown, mapping = aes(x = Month, fill = PaymentPlan)) +  
  geom_bar(position = "fill") +  
  scale_fill_manual(values = c("orchid", "maroon4"))
```



- To access a list of available colors in R, use the `colors()` function.

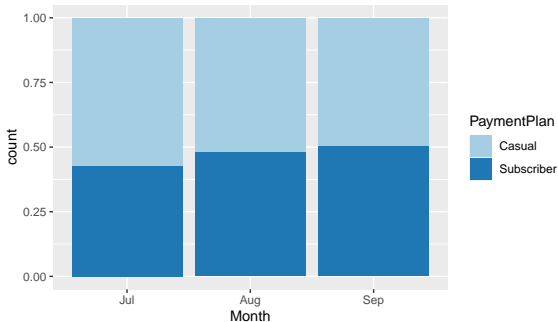
## Using Palettes

We can also choose colors from a list of predefined color palettes:

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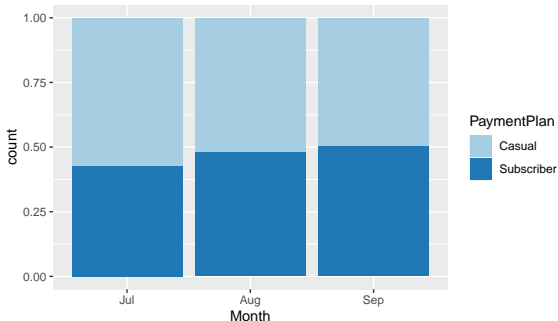
```
ggplot(data = biketown, mapping = aes(x = Month, fill = PaymentPlan)) +  
  geom_bar(position = "fill") +  
  scale_fill_brewer(type = "qual", palette = 3)
```



## Using Palettes

We can also choose colors from a list of predefined color palettes:

```
ggplot(data = biketown, mapping = aes(x = Month, fill = PaymentPlan)) +  
  geom_bar(position = "fill") +  
  scale_fill_brewer(type = "qual", palette = 3)
```



- Type can be seq (for sequential), div (for diverging), or qual (for qualitative)
- Each type has around 8-10 different palettes (numbered 1, 2, 3, ...)

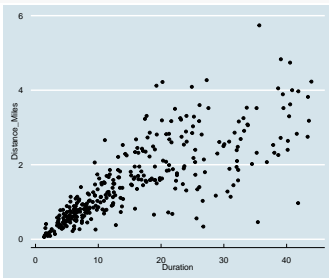
## Change Theme

We can also control the styling of other plot elements via `theme`

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We can also control the styling of other plot elements via theme

```
ggplot(data = biketown_sample,  
       mapping = aes(x = Duration,  
                      y = Distance_Miles))  
geom_point()+  
theme_economist()
```



```
ggplot(data = biketown_sample,  
       mapping = aes(x = Duration,  
                      y = Distance_Miles))  
geom_point()+  
theme_bw()
```

