## Introduction to the Grammar of Graphics

Prof. Wells

STA 209, 1/30/23

### Outline

In this lecture, we will...

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- Discuss the Grammar of Graphics
- Decompose particular graphics using the GG paradigm
- Introduce the ggplot2 package for R graphics

#### Section 1

The Grammar of Graphics

# The Guiding Principle

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<u>data</u>						
Planet Name						
Planet Diameter						
Planet Name						

geometric object
bar
bar
bar

## The Guiding Principle

data Planet Name

A statistical graphic is a mapping of data variables to aesthetic attributes of geometric objects. aesthetics

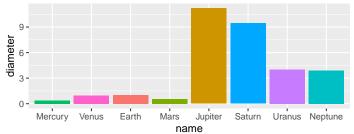
geometric object

har

```
Planet Diameter
                                         y height
                                                              bar
                    Planet Name
                                          color
                                                              har
ggplot(data = planets_df) +
```

x position

```
geom_bar(stat = "identity", mapping = aes(x = name, y = diameter, fill = name)
```



• data: data frame that contains the raw data and variables of interest

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   i.e. specifying particular colors or shapes
- guide: a legend to help user convert visual display back to the data

# Plotting the Planets

Consider the planets data frame, planets\_df:

name	type	diameter	rotation	rings	distance
Mercury	Terrestrial planet	0.382	58.64	FALSE	0.4
Venus	Terrestrial planet	0.949	-243.02	FALSE	0.7
Earth	Terrestrial planet	1.000	1.00	FALSE	1.0
Mars	Terrestrial planet	0.532	1.03	FALSE	1.5
Jupiter	Gas giant	11.209	0.41	TRUE	5.2
Saturn	Gas giant	9.449	0.43	TRUE	9.5
Uranus	Gas giant	4.007	-0.72	TRUE	19.2
Neptune	Gas giant	3.883	0.67	TRUE	30.1

## Plotting the Planets

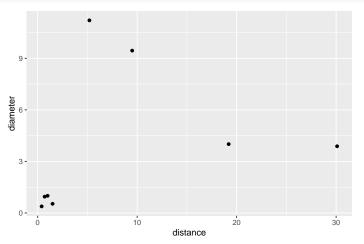
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Describe how to create a plot of distance vs. diameter.

# Plotting the Planets

```
ggplot(data = planets_df, mapping = aes(x = distance, y = diameter)) +
  geom_point()
```



## Decomposing Graphics

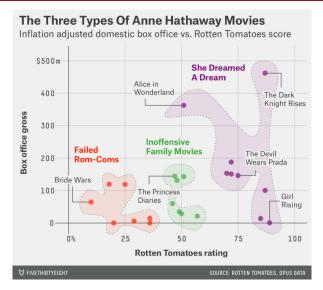
Let's get some practice decomposing visualizations using the grammar of graphics. For each of images on the next slides, we'll answer the following:

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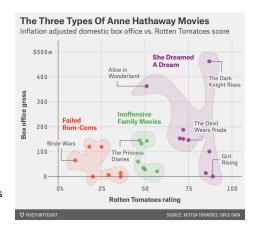
- What is the story this graphic is telling?
- What are the variables here?
- What geom are the variables mapped to?
- What are the aesthetics of the geom? Which variable sets the value of that aesthetic?
- 6 What additional context does this graphic provide?

## Example 1 Graphic



#### Example 1

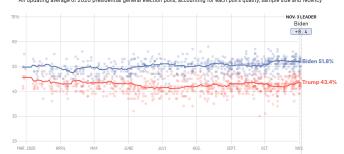
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## Example 2 Graphic



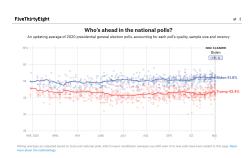
# Who's ahead in the national polls? An updating average of 2020 presidential general election polls, accounting for each poll's guality, sample size and recency



Polling averages are adjusted based on state and national polls, which means candidates' averages can shift even if no new polls have been added to this page. Read more about the methodology.

#### Example 2

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- What are the variables here?
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- Include a legend to translate from aesthetics to variables.
- Specify your data source for reproducibility/verification.
- Minimize/eliminate extraneous elements that do not serve main purpose.

### Section 2

The ggplot2 Package

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• The code for graphics will (almost) always take the following general form:

```
ggplot(data = ---, mapping = aes(---)) +
  geom_---(---)
```

• For brevity, the above code can also be written as:

```
ggplot(---, aes(---)) + geom_---(---)
```

• R will assume that the first argument is the data argument and the second argument is the mapping argument.

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- What advantages does ggplot2 (and the Grammar of Graphics) have over these other tools?

- Several other applications have capability of plotting graphics.
  - Excel and Google Spreadsheets each have separate buttons to produced bar plots, scatter plots, line plots, etc. from data sets.
- What advantages does ggplot2 (and the Grammar of Graphics) have over these other tools?
  - Control
  - Intentionality
  - Consistency
  - · Ability to create publication quality graphs with minimal tuning

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  - ① Scatterplots (geom\_point)
  - 2 Linegraphs (geom\_line)
  - Histograms (geom\_histogram)
  - 4 Boxplots (geom\_boxplot)
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  - 2 Linegraphs (geom\_line)
  - Histograms (geom\_histogram)
  - 4 Boxplots (geom\_boxplot)
  - Barplots (geom\_bar)
- Other common graph types you may encounter:
  - Violin plots (geom\_violin)
  - Interpolation (geom\_smooth)
  - Geographic maps (geom\_map)
  - Polygon areas (geom\_poly)
  - Density plots (geom\_density)

• We'll use a common data set to investigate each graph: the Portland Biketown data: biketown <- read\_csv("biketown.csv")

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  - Users can purchase a single-ride fare, a day pass, or an annual membership. They can borrow a bike from any bike station, and return the bike to any station.

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  - Users can purchase a single-ride fare, a day pass, or an annual membership. They can borrow a bike from any bike station, and return the bike to any station.
  - Bike stations automatically log data on each trip.
  - The biketown data was obtained from the BiketownPDX website and contains a random sample of all bike share rides between July and September, 2017.

#### Biketown Preview

• First, let's preview the data frame:

#### glimpse(biketown)

```
## Rows: 9.999
## Columns: 19
## $ RouteID
                     <dbl> 4074085, 3719219, 3789757, 3576798, 3459987, 3947695,~
## $ PaymentPlan
                     <chr> "Subscriber". "Casual". "Casual". "Subscriber". "Casua"
                     <chr> "SE Elliott at Division", "SW Yamhill at Director Par~
## $ StartHub
## $ StartLatitude
                     <dbl> 45.50513, 45.51898, 45.52990, 45.52389, 45.53028, 45.~
## $ StartLongitude
                     <dbl> -122.6534, -122.6813, -122.6628, -122.6722, -122.6547~
## $ StartDate
                     <chr> "8/17/2017", "7/22/2017", "7/27/2017", "7/12/2017", "~
## $ StartTime
                     <time> 10:44:00, 14:49:00, 14:13:00, 13:23:00, 19:30:00, 10~
## $ EndHub
                     <chr> "Blues Fest - SW Waterfront at Clay - Disabled", "SW ~
## $ EndLatitude
                     <dbl> 45.51287, 45.52142, 45.55902, 45.53409, 45.52990, 45.~
## $ EndLongitude
                     <dbl> -122.6749, -122.6726, -122.6355, -122.6949, -122.6628~
## $ EndDate
                     <chr> "8/17/2017", "7/22/2017", "7/27/2017", "7/12/2017", "~
## $ EndTime
                     <time> 10:56:00, 15:00:00, 14:42:00, 13:38:00, 20:30:00, 10~
## $ TripType
                     ## $ BikeID
                     <dbl> 6163, 6843, 6409, 7375, 6354, 6088, 6089, 5988, 6857,~
## $ BikeName
                     <chr> "0488 BIKETOWN", "0759 BIKETOWN", "0614 BIKETOWN", "0~
## $ Distance Miles
                     <dbl> 1.91, 0.72, 3.42, 1.81, 4.51, 5.54, 1.59, 1.03, 0.70,~
## $ Duration
                     <dbl> 11.500, 11.383, 28.317, 14.917, 60.517, 53.783, 23.86~
## $ RentalAccessPath <chr> "keypad", "keypad", "keypad", "keypad", "keypad", "key
## $ MultipleRental
                     <lg> FALSE, FALSE, FALSE, FALSE, TRUE, FALSE, FALSE~
```

What do the first few entries look like?

#### What do the first few entries look like?

head(biketown)

```
## # A tibble: 6 x 19
##
    RouteID Payme~1 Start~2 Start~3 Start~4 Start~5 Start~6 EndHub EndLa~7 EndLo~8
##
      <dbl> <chr>
                    <chr>
                             <dbl>
                                     <dbl> <chr>
                                                  <time>
                                                          <chr>
                                                                   <dbl>
                                                                          <dbl>
## 1 4074085 Subscr~ SE Ell~
                              45.5
                                     -123. 8/17/2~ 10:44
                                                          Blues~
                                                                    45.5
                                                                          -123.
## 2 3719219 Casual SW Yam~
                             45.5 -123. 7/22/2~ 14:49
                                                         SW 2n~
                                                                   45.5
                                                                          -123.
## 3 3789757 Casual NE Hol~
                             45.5 -123. 7/27/2~ 14:13
                                                         NE Al~
                                                                   45.6
                                                                          -123.
## 4 3576798 Subscr~ NW Cou~ 45.5 -123. 7/12/2~ 13:23
                                                         NW Ra~
                                                                   45.5
                                                                          -123.
## 5 3459987 Casual NE 11t~
                           45.5 -123. 7/3/20~ 19:30 NE Ho~
                                                                   45.5
                                                                          -123.
## 6 3947695 Casual SW Moo~
                              45.5
                                     -123. 8/8/20~ 10:01
                                                          SW 3r~
                                                                    45.5
                                                                          -123.
## # ... with 9 more variables: EndDate <chr>. EndTime <time>. TripType <1gl>...
## #
      BikeID <dbl>, BikeName <chr>, Distance Miles <dbl>, Duration <dbl>,
      RentalAccessPath <chr>>. MultipleRental <lgl>. and abbreviated variable
## #
      names 1: PaymentPlan, 2: StartHub, 3: StartLatitude, 4: StartLongitude,
## #
## #
      5: StartDate, 6: StartTime, 7: EndLatitude, 8: EndLongitude
## # i Use `colnames()` to see all variable names
```

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• To access 1 variable of a data set, separate the dataframe and variable name with \$ biketown\$Distance Miles

```
[1]
                                 1.81
                                        4.51
                                              5.54
                                                     1.59
                                                            1.03
                                                                   0.70
                                                                          1.72
                                                                                 1.79
##
            1.91
                   0.72
                          3.42
                                                                                        3.15
##
      [13]
            0.81
                   0.55
                          5.78
                                 0.41
                                       3.76
                                              2.22
                                                     1.77
                                                            4.96
                                                                   3.19
                                                                          2.56
                                                                                 2.55
                                                                                        0.68
      [25]
            0.59
                   0.71
                          3.15
                                 5.89
                                       1.34
                                              1.56
                                                     3.50
                                                            1.81
                                                                   2.74
                                                                          4.56
                                                                                 3.99
                                                                                        1.03
##
##
      [37]
            1.51
                   2.87
                          2.60
                                 1.48
                                       0.96
                                              2.82
                                                     0.66
                                                            0.37
                                                                   2.38
                                                                          5.92
                                                                                 1.27
                                                                                        0.78
##
      [49]
            0.79
                   3.38
                          1.73
                                 3.64
                                        1.40
                                              2.61
                                                     1.85
                                                            1.04
                                                                   1.55
                                                                          0.63
                                                                                 3.41
                                                                                        4.94
##
      [61]
            3.93
                   0.40
                          1.00
                                 7.19
                                        7.15
                                              0.96
                                                     0.33
                                                            0.79
                                                                   2.80
                                                                          1.08
                                                                                 2.27
                                                                                        0.62
##
      [73]
            0.50
                   2.15
                          0.23
                                 3.06
                                        1.85
                                              5.00
                                                     0.42
                                                            3.05
                                                                   0.42
                                                                          1.00
                                                                                 4.09
                                                                                        0.45
      [85]
            2.53
                   0.66
                          0.26
                                 1.89
                                        1.63
                                              0.99
                                                     1.62
                                                            1.87
                                                                   6.73 12.95
                                                                                        0.43
##
                                                                                 3.44
      [97]
            0.82
                   0.72
                          1.51
                                 1.70
                                       0.34
                                              0.55
                                                     2.84
                                                            1.31
                                                                   2.78
                                                                          1.09
                                                                                 1.25
                                                                                        5.04
##
##
    [109]
            1.18
                   1.15
                          1.62
                                 0.63
                                       3.88
                                              4.67
                                                     1.25
                                                            0.34
                                                                   3.11
                                                                          5.29
                                                                                 1.00
                                                                                        1.67
    [121]
            0.61
                   0.47
                          0.68
                                 0.66
                                       0.71
                                              0.02
                                                     0.87
                                                            1.61
                                                                   4.50
                                                                          1.47
                                                                                 4.53
                                                                                        0.10
##
##
    [133]
            0.25
                   5.50
                          2.05
                                 4.98
                                       0.66
                                              0.12
                                                     4.79
                                                            0.47
                                                                   4.19
                                                                          0.43
                                                                                 1.57
                                                                                        0.27
##
    [145]
            0.17
                   1.08
                          0.36
                                 5.16
                                       6.74
                                              2.54
                                                     0.48
                                                            0.91
                                                                   1.80
                                                                          0.19
                                                                                 2.71
                                                                                        1.32
##
    Γ157]
            2.75
                   1.14
                          0.65
                                 2.58
                                       3.77
                                              0.66
                                                     3.55
                                                            1.37
                                                                   0.98
                                                                          1.41
                                                                                 1.01
                                                                                        1.87
##
    [169]
            0.51
                   0.37
                          1.12
                                 0.84
                                       0.55
                                              0.12
                                                     3.64
                                                            4.69
                                                                   0.15
                                                                          2.94
                                                                                 5.06
                                                                                        1.24
##
    [181]
            0.83
                   2.32
                          1.25
                                 2.82
                                        0.61
                                               1.80
                                                     1.41
                                                            1.16
                                                                   1.09
                                                                          2.03
                                                                                 1.34
                                                                                        0.55
    [193]
            0.45
                   4.79
                          4.30
                                 0.45
                                       2.05
                                              0.71
                                                     0.16
                                                            0.31
                                                                          1.49
                                                                                 3.27
##
                                                                   0.01
                                                                                        3.11
##
    [205]
            0.78
                   2.62
                          0.63
                                 2.09
                                        1.83
                                              0.35
                                                     0.82
                                                            1.39
                                                                   2.39
                                                                          0.58
                                                                                 0.36
                                                                                        0.28
    [217]
            1.65
                   0.79
                          1.90
                                 1.27
                                        3.71
                                              2.96
                                                     7.12
                                                            3.20
                                                                   0.40
                                                                          1.50
                                                                                 0.93
                                                                                        1.97
##
    [229]
            0.73
                   0.68
                          0.91
                                 3.20
                                        2.27
                                              2.67
                                                     2.37
                                                            0.05
                                                                   0.82
                                                                          2.50
                                                                                 2.17
                                                                                        0.44
##
                                        1.78
##
    [241]
            2.79
                   0.07
                          0.66
                                 1.93
                                              0.59
                                                     1.54
                                                            1.59
                                                                   1.47
                                                                          0.62
                                                                                 1.63
                                                                                        2.68
##
    [253]
            0.27
                   1.46
                          0.68
                                 0.16
                                       0.42
                                              0.55
                                                     1.47
                                                            0.27
                                                                   2.02
                                                                          0.85
                                                                                 0.63
                                                                                        0.58
##
    [265]
            0.60
                   0.56
                          2.12
                                 1.48
                                       0.60
                                              0.88
                                                     0.62
                                                            0.48
                                                                   2.55
                                                                          0.82
                                                                                 0.97
                                                                                        3.45
```

To determine the variable type in R, use class

```
class(biketown$Distance_Miles)
## [1] "numeric"
class(biketown$PaymentPlan)
```

```
## [1] "character"
```

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```

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class(biketown\$PaymentPlan)

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```
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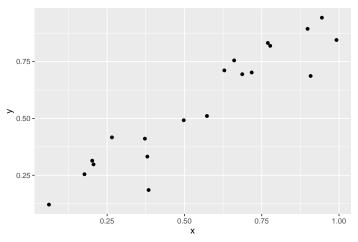
```
##
    [1] "RouteID"
                             "PaymentPlan"
                                                 "StartHub"
                                                                      "StartLatitude"
    [5]
                             "StartDate"
                                                 "StartTime"
                                                                      "EndHub"
##
        "StartLongitude"
##
    [9]
        "EndLatitude"
                             "EndLongitude"
                                                 "EndDate"
                                                                      "EndTime"
   [13] "TripType"
                             "BikeID"
                                                 "BikeName"
                                                                      "Distance Miles"
   [17] "Duration"
                             "RentalAccessPath"
                                                 "MultipleRental"
```

Section 3

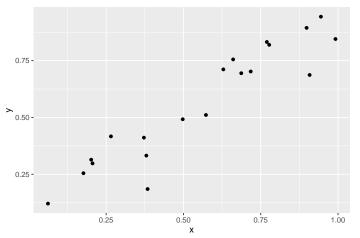
Types of Graphics

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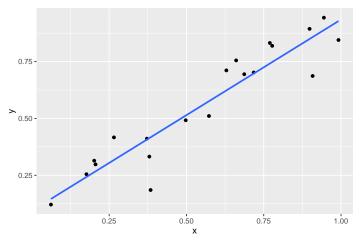


Scatterplots show relationships between a pair of quantitative variables.



In particular, we are often interested in linear relationships.

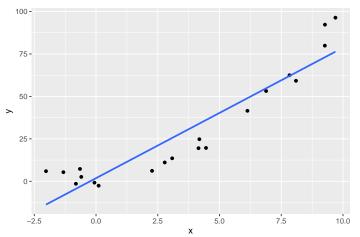
• Scatterplots show relationships between a pair of **quantitative** variables.



In particular, we are often interested in linear relationships.

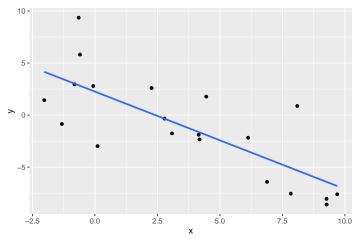
Two variables have a positive relationship provided the values of one increase as the
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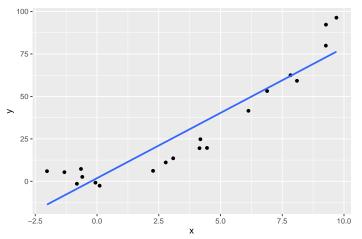
 Two variables have a negative relationship provided the values of one decrease as the values of the other also increase.

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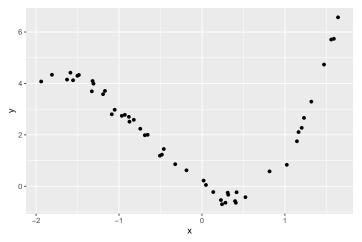
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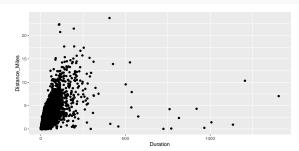
# Creating Scatterplots

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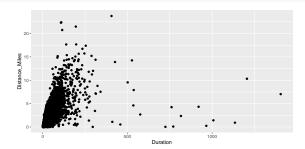
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ggplot(data = biketown, mapping = aes(x = Duration, y = Distance_Miles)) +
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Problems with the graphic?

## Overplotting

 Overplotting occurs when a large number of points are plotted in close proximity, making it difficult to accurately distinguish true number of points in a region.

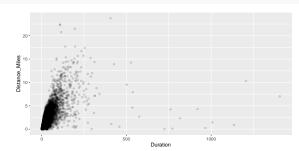
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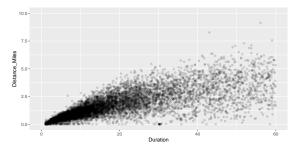
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ggplot(data = biketown, mapping = aes(x = Duration, y = Distance_Miles)) +
geom_point(alpha = 0.15)
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```
ggplot(data = biketown, mapping = aes(x = Duration, y = Distance_Miles)) +
  geom_point(alpha = .15)+
  scale_x_continuous(limits = c(0, 60))+
  scale_y_continuous(limits = c(0, 10))
```

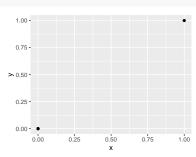


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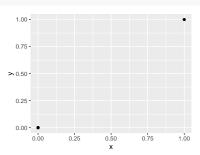
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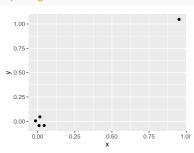
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It looks like there are just 2 observations!

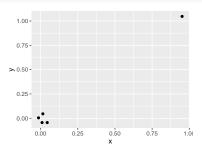
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• To jitter points, use the layer geom\_jitter(width = ..., height = ...) instead of geom points()